

MA1113 - SINGLE VARIABLE CALCULUS I (4-0)

Prerequisite: Algebra

Text: Calculus (Early Transcendentals), Eighth Edition, by James Stewart, Cengage, ISBN 978-1-285-74155-0.

| HOURS | TOPICS | SECTION | HOMEWORK |
|-------|--|------------|----------------------|
| 2-2 | Real Numbers, Sets, Inequalities, Absolute Value | Appendix A | 1-29*, 47-55* |
| 1-3 | Coordinate Geometry and Lines | Appendix B | 1-9*, 21-27*, 43-51* |
| 1-4 | Trigonometry | Appendix D | 1-15* |
| 1-5 | Four Ways to Represent a Function | 1.1 | 3-9*, 27-35* |
| 1-6 | Essential Elementary Functions | 1.2 | 1,2 |
| | New Functions from Old | 1.3 | 1-5*, 9-21, 33-41* |
| 1-7 | Exponentials | 1.4 | 1,2,17-21 |
| 1-8 | Inverse Functions and Logarithms | 1.5 | 21-26,39-46,61-62 |
| 1-9 | Limit Concept; Limit Calculation Laws | 2.1-2.3 | 2.3: 1-31* |
| 1-10 | Continuity | 2.5 | None |
| 1-11 | Limits at Infinity; Horizontal Asymptotes | 2.6 | 15-29* |
| 1-12 | Derivatives and Rates of Change | 2.7 | None |
| 1-13 | Derivatives as Functions | 2.8 | 21-29* |
| 1-14 | Derivatives of Polynomials and Exponential Functions | 3.1 | 3-41* |
| 1-15 | Product and Quotient Rules | 3.2 | 3-35* |
| 1-16 | Derivatives of Trigonometric Functions | 3.3 | 1-21*,27,29 |
| 2-18 | The Chain Rule | 3.4 | 7-45* |
| 1-19 | Implicit Differentiation | 3.5 | 5-15*,25,27 |
| 1-20 | Logarithmic Differentiation | 3.6 | 3-25*,45-49* |
| 2-22 | Related Rates | 3.9 | 1-19* |
| 2-24 | Linear Approximations; Differentials; Error Estimation | 3.10 | 1-4,15-18,23-26* |
| 0-24 | Derivatives of Hyperbolic Functions | 3.11 | None |
| 1-25 | Maximum and Minimum Values | 4.1 | 29-43*,51-59* |
| 1-26 | Optimization Problems | 4.7 | 1,3,9,11,12,15,21,23 |
| 1-27 | Mean Value Theorem | 4.2 | 5-13 |
| 1-28 | Indeterminate Forms and L'Hospital's Rule | 4.4 | 9-27* |
| 1-29 | Anti-derivatives | 4.9 | 1-17*,27-33* |
| 1-30 | Areas and Distances | 5.1 | None |
| 1-31 | The Definite Integral | 5.2 | None |
| 1-32 | The Fundamental Theorem of Calculus | 5.3 | 9-35* |
| 1-33 | Indefinite Integrals and Net Change Theorem | 5.4 | 5-15*,27-35* |
| 2-35 | The Substitution Rule (Change of Variable) | 5.5 | 7-33*,59-65* |
| 2-37 | Integration by Parts | 7.1 | 1-17* |
| 1-38 | How Derivatives Affect Graph Shapes | 4.3 | 9-21* |
| 1-39 | Newton's Method | 4.8 | None |
| 6-45 | Reviews, Exams, Holidays | | |

* Do odd numbered problems in this range.

Course Objectives

Upon completion of this course, the student should have the following skills.

Functions and limits

- Use real numbers, inequalities involving real numbers and their absolute values, the trigonometric functions, and the radian measure of angles.
- Be able to move back and forth between the descriptions of a function by an equation, a table, a graph, and by words.
- Be able to use exponential functions, sketch their graphs, and define the number e .
- Define what it means for a function to be one-to-one and determine whether a function has an inverse or not and sketch its inverse if it does.
- Be able to use logarithmic functions, sketch their graphs, and define the relationship between the natural exponential and natural logarithmic functions.
- State in words what it means for a function to have a limit, be able to calculate limits, and be able to find the vertical and horizontal asymptotes of a function.
- State in words what it means for a function to be continuous and be able to find limits for continuous functions.

Derivatives

- Relate the notions of tangent to a curve, velocity, and rate of change, and illustrate them in a sketch.
- State the definition of derivative as the limit of a difference quotient and explain how the derivative itself can be regarded as a function.
- Be able to find derivatives of polynomials and exponential functions.
- State the product and quotient rules for differentiation and be able to use them to differentiate functions.
- Know the derivatives of sine and cosine and be able to use the quotient rule to determine the derivatives of the remaining four trigonometric functions.
- State the chain rule and use it to differentiate functions obtained by composition.
- Use the differentiation rules to differentiate implicitly, and to find higher order derivatives.
- Be able to differentiate logarithmic functions, and functions involving them.
- Define the hyperbolic functions and be able to differentiate them.

Applications of Differentiation

- Be able to solve related rates problems. Understand them as an application of the chain rule.
- Understand the connection between the derivative, the tangent line to the graph of a function, the linearization of a function, and the differential of a function.
- Use the differential (or linearization) to solve “small change” and applied approximation problems.
- Be able to state the Mean Value Theorem and give some of its consequences.
- Describe how the signs of the first and second derivatives of a function affect the shape of its graph.
- Define and recognize the various forms of indeterminate forms, and use L'Hospital's Rule to determine their limits.
- Be able to set up and solve optimization problems using calculus methods.
- Be able to describe Newton's method geometrically, and to use it to iteratively approximate the zeros of functions.
- Define what the antiderivative of a function is and be able to find it for reasonable functions.

Integral Calculus

- Describe the connection between the problems of finding areas and distances travelled, and how both problems lead to the same limit.
- Know and be able to work with the properties of definite integrals.
- State the Fundamental Theorem of Calculus in words, describe how it connects integral and differential calculus, and how it helps in finding antiderivatives and in evaluating definite integrals.
- Define the indefinite integral of a function and state its relation to the antiderivative.
- Be able to use the Substitution Rule to evaluate definite and indefinite integrals.
- Be able to use integration by parts to evaluate appropriate integrals.